Please sign your name for the honor pledge:

9/25/2007
MA371 Intro. To Prob. \& Stats.
Quiz 3

Name:
(25 Points Total)
I. Dr. L. has twelve cans of cat food for Kitteny Thang (KT) and Hep Kat. The twelve cans, 5 tuna flavor and 7 liver flavor, are stored in a bin on a top shelf. Each day Dr. L. reaches into the bin, randomly selects two cans of cat food and splits the contents for the cats (i.e. each cat gets $1 / 2$ of each can). Please answer the following. Please show your answers in both combinatorial and decimal form. (3 points each -6 points total)
(a) KT loves tuna! Is there a better than $50 \%$ chance that she will get some tuna on the first feeding day with these 12 cans? I.e. find the probability that KT will get some tuna on the first day Dr. L. selects cat food.
(b) What is the probability that the $8^{\text {th }}$ can of cat food chosen will be the $3^{\text {rd }}$ can of tuna chosen (i.e. the second can chosen on the $4^{\text {th }}$ day will be tuna)?
II. The discrete random variable $X$ has probability mass function $f(x)=\frac{x}{55}$ for $x=1,2, \ldots, 10$. Please find the following being sure to show all intermediate steps. (3 points each, 6 total)
(a) $P(X>8)$
(b) $P(X>8 \mid X \geq 2)$
III. Suppose that $A$ and $B$ are events in a sample space, $S$, and that $P(A)=0.70, P(B)=0.50$, and $P(A \cup B)=0.80$. Please answer the following. For full credit on each problem you must show at least one intermediate step for any probability computations. (6 points total)
(a) Find $P(B \mid A)$ (3 points)
(b) Are $A$ and $B$ independent events? Why or why not? (3 points)
IV. A store sells three brands of DVD players. The least expensive brand, $B_{1}$, accounts for $55 \%$ of all sales and the other two brands, $B_{2}$ and $B_{3}$, account for $25 \%$ and $20 \%$ of sales, respectively. The chances of needing a repair during the warranty period are $10 \%$ for $B_{1}, 5 \%$ for $B_{2}$ and $2 \%$ for $B_{3}$. Let $R$ be the event that a randomly selected purchaser bought a DVD player that needs a repair during the warranty period, $B_{1}$ be the event they purchased a DVD player of brand type $B_{1}$, etc. Please answer the following. Please write all probability computations in terms of the given event names. (7 points total)
(a) Find $P(R)$. (3 points)
(b) Without computing $P\left(B_{2} \mid R\right)$, describe using a complete English sentence with no abbreviations for event names the probability this represents (i.e. "This is the probability of ......."). (1 point)
(c) Now find $P\left(B_{2} \mid R\right)$.(3 points)

