

Pledge:

1/2/2010
Dr. Lunsford

MATH361 Calculus III
Quiz 2

Name: _____
(30 Points Total)

Please show all work on this quiz.

Problem I. Given the points $P(2, 1, 5)$, $Q(-1, 3, 4)$, and $R(3, 0, 6)$ please answer the following: (8 points total)

(a) Find a unit vector orthogonal (i.e. perpendicular) to the plane through the three points. (5 points)

(b) Find the area of the triangle $\triangle PQR$. (3 points)

Problem II. Consider the plane given by the equation $2x - 3y + 4z = 4$ and the line given by the parametric equations $x = 3 + 3t$, $y = 2 - 2t$, and $z = 1 - 3t$. Please answer the following: (11 points total)

(a) Give a vector perpendicular to the plane. (2 points)

(b) Is the point $P(3, 2, 1)$ on the plane? Why or why not? (3 points)

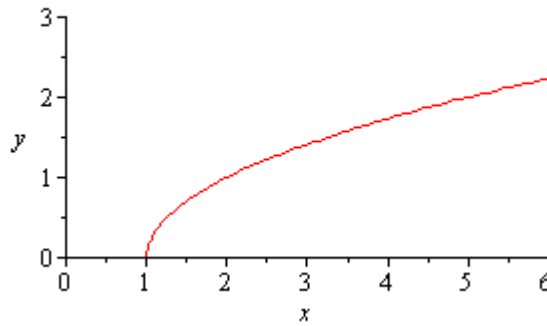
(c) Find a vector parallel to the line. (2 points)

(d) Does the line lie on the plane? Why or why not? (4 points)

Problem III. Consider a point that moves along the plane curve given by $\mathbf{r}(t) = (1+t)\mathbf{i} + \sqrt{t}\mathbf{j}$. To your right you are given a graph of this curve. Please answer the following: (6 points total)

(a) Sketch the position vector $\mathbf{r}(1)$ on the graph. (2 points)

(b) Sketch the tangent (velocity) vector to the graph at $t = 4$. (4 points)



Problem IV. Consider the space curve given by $\mathbf{r}(t) = \cos(3t)\mathbf{i} + e^{3t}\mathbf{j} + 2\sin(2t)\mathbf{k}$. Find the unit tangent vector to the curve at $t = 0$. (5 points)