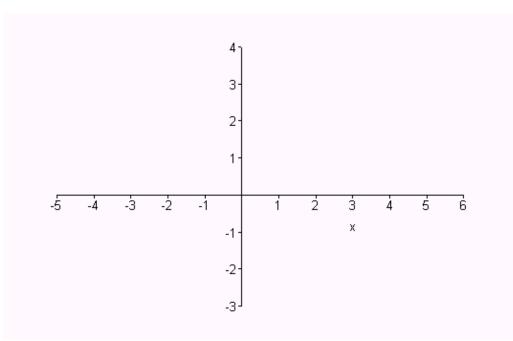
For all limits on this test, determine if the limit exists as a number, exists in the infinite sense, or does not exist. If the limit exists find its value.

Problem I. Use the graph of the function f below to answer the following questions. (3 points each – 27 total)



$$f(0) = \underline{\qquad} f(3) = \underline{\qquad} \lim_{x \to -2^{+}} f(x) = \underline{\qquad} \lim_{x \to 5^{+}} f(x) = \underline{\qquad} \lim_{x \to 5^{+}} f(x) = \underline{\qquad} \lim_{x \to -2^{-}} f(x) = \underline{\qquad} \lim_{x \to -2^{-}} f(x) = \underline{\qquad} \lim_{x \to -\infty} f(x) = \underline{\qquad} \lim$$

For the remaining questions, please write "true" or "false", according to which is correct about the statement, in the space provided next to each statement.

_____ f is continuous at x = 5. _____ f is continuous from the right at x = -2. _____ f is continuous on the interval [-2,5) _____ f'(-4) < f'(0)

Problem II. Determine if the function given by $f(x) = \begin{cases} \frac{\sin x}{x}, & x < 0 \\ x^2 + 1, & 0 \le x \end{cases}$ is continuous at x = 0. You must

clearly justify your answer using the definition of continuity at a point. (6 points)

Problem III. Find the indicated limits – clearly indicate your answers. *You do not need to show any intermediate steps for these problems*. Very little partial credit will be given for these problems. (2 points each, 16 total)

1.
$$\lim_{x \to 2^{-}} \frac{x}{2-x}$$

$$2. \lim_{x \to \infty} \frac{7 - 8x^2}{3x^2 + 11}$$

3.
$$\lim_{x \to -1} 4x^{13} - 9x^{15} + 11x^{14}$$

4.
$$\lim_{x \to -\infty} 4x^{13} - 9x^{15} + 11x^{14}$$

$$5. \quad \lim_{x \to -\infty} \tan^{-1}(x)$$

$$6. \lim_{x \to \infty} \ln \left(\frac{1}{x} \right)$$

7.
$$\lim_{x\to 0^-} e^{1/x}$$

$$8. \quad \lim_{x \to 2^+} \sqrt{2 - x}$$

<u>Problem IV.</u> Consider the following table of values given below. Please answer the following questions (3 points each, 6 total)

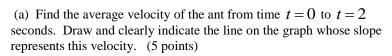
(a) From the numerical evidence, what is $\lim_{x \to 2} f(x)$?

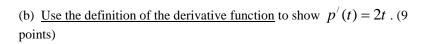
				2.005		
f(x)	-4.013	-4.006	-4.002	-3.997	-3.991	-3.839

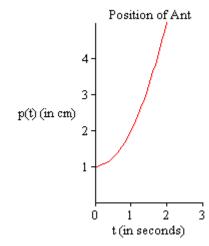
(b) Is it possible that $\lim_{x\to 2} f(x)$ does not exist or equals some other number than your answer in part (a)? Why or why not?

Problem V. An ant walks along a ruler. The ant's position is given by the function $p(t) = t^2 + 1$ where

p(t) is in centimeters and t is in seconds. A graph of this position function is given below. Please answer the following questions. (20 points total)







(c) Find the velocity of the ant at time t=1 seconds. Find the equation of the line whose slope represents this velocity. Accurately draw and clearly indicate the line on the graph. (6 points)

<u>Problem VI.</u> Find the indicated limits. You must show at least one intermediate step to receive full credit. (5 points each -25 points total)

1.
$$\lim_{u \to 0} u^2 \cos u^{-2}$$

Hint: What is a nice theorem to use if you are between a rock and a hard place?

$$2. \lim_{t \to 3} \frac{\frac{1}{t^2 + 1} - \frac{1}{10}}{t - 3}$$

3.
$$\lim_{x \to -1^+} \frac{x^2 + 3x + 2}{2x^2 + x - 1}$$

4.
$$\lim_{x \to -\infty} \frac{\sqrt{x^2 - 9}}{2x - 6}$$

5.
$$\lim_{x \to -\pi^+} \frac{x + \frac{\pi}{2}}{\sin x}$$