Pledge:

MATH261 Calculus I Ouiz 3

I. Basic limits. Find the exact value of the following limits (i.e. not a calculator approximation). You are not required to show an intermediate step for these problems. (2 points each – no partial credit, 8 points total)

1.
$$\lim_{t \to \infty} 10^7 t^3 - 11t^4 + 10^6 t^2$$

2.
$$\lim_{x \to 1^+} \frac{x-2}{x-1}$$

3.
$$\lim_{x \to \infty} \frac{3x - 4x^3}{6 + 2x^3}$$

4.
$$\lim_{x \to -\infty} \frac{x-1}{x^3 + 7}$$

II. More interesting limits. Find the exact value of the following limits (i.e. not a calculator approximation). For each limit you must show at least one intermediate step for full credit. (5 points each, 10 points total)

1.
$$\lim_{w \to 4^{-}} \frac{-8 + 6w - w^{2}}{w^{2} - 8w + 16}$$

2.
$$\lim_{x \to -\infty} \frac{4x + 7}{\sqrt{9x^2 + x - 4}}$$

III. Let
$$f(x) = \begin{cases} \frac{1}{x+2} & , x < -2 \\ x & , -2 \le x < 2 \end{cases}$$
. Please answer the following questions using this function. (4 points each, 12 total)

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(a) Is f continuous at x = 2? You must show all work to justify your answer.

(b) Is x = -2 a vertical asymptote of the function? Again show all work to justify your answer.

(c) Does f have a horizontal asymptote? Why or why not? Please show all work to justify your answer.