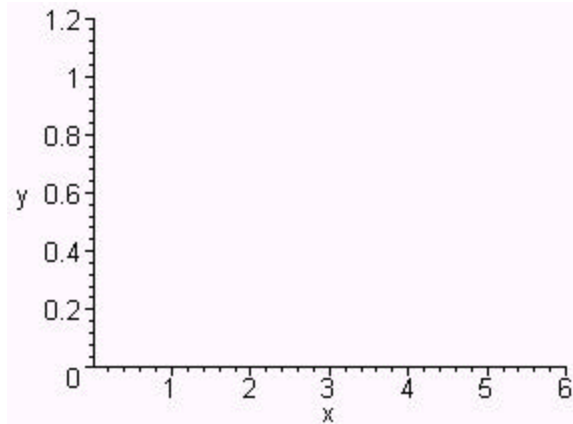


I. Let  $X$  be a continuous uniform random variable with p.d.f given by  $f(x) = \frac{1}{b-a}$  for  $a \leq x \leq b$ . Please answer the following:

(a) Using the definition, prove that the mean of this distribution is  $\frac{a+b}{2}$  (5 points)

(b) Now suppose that  $a = 2$  and  $b = 5$ . Find the cumulative distribution function (c.d.f.) for  $X$ . Clearly indicate your answer. (5 points)

(c) Still assuming that  $a = 2$  and  $b = 5$ , graph the p.d.f. and the c.d.f. on the axes provided to the right. Be sure to indicate which graph is the p.d.f. and which graph is the c.d.f. (5 points)



II. Suppose that the random variable  $X$  has the p.d.f.  $f(x) = \frac{3}{16}\sqrt{x}$  for  $0 \leq x \leq 4$ . A graph of this p.d.f. is given below. Find  $P(1 < X < 6)$  and show this probability on the graph. (5 points)

