

Each problem counts four points. Neatly show all of your work and clearly indicate your answers.

I. Let X be a random variable and $f(x) = c(x+1)^2$, $x = 0, 1, 2, 3, 4$. Find a value for the constant C so that f is a p.m.f. for X .

II. Let Y be a random variable and suppose that $E[Y - 4] = 10$ and $E[(Y - 4)^2] = 105$. Find each of the following:

(a) m_Y

(c) s_Y^2

III. Suppose there are 10 defective items in a lot of 100 items. An inspector tests 20 items selected at random. Let the random variable X denote the number of defective items in the 20 tested. Please answer the following:

(a) How is the random variable X distributed? You should provide the p.m.f. for the random variable and the possible values of X .

(b) Find the probability that at least one defective item is found in the 20 items inspected.

BONUS: On average, how many defective items should the inspector expect to find in the 20 items tested? (2 points)