

Suppose the discrete random variable  $X$  has probability mass function (p.m.f.) given by

$$f(x) = \frac{4-x}{6}, x = 1, 2, 3. \text{ Use this information to answer the following questions.}$$

- (a) Draw a bar graph of the p.m.f. of  $X$ . Clearly label your axes. (3 points)
- (b) Find the probability that  $X$  is at most two. Clearly write this probability in terms of the random variable. Also show how you use the p.m.f. to compute this probability. (3 points)
- (c) Find the mean of the distribution for  $X$ . Clearly show all work including what formula you are using (and how you are plugging into that formula) for this computation. (4 points)
- (d) Find  $E[X^2]$ . Clearly show all of your work. (3 points)
- (e) Find the standard deviation of the distribution for  $X$ . Clearly show all work including what formula you are using (and how you are plugging into that formula) for this computation. (4 points)
- (f) Suppose we define a new random variable  $Y$  by  $Y = -2X + 7$ . Find the mean and variance of  $Y$ . Clearly indicate your answers. (3 points)